# The University of Western Ontario – Department of Statistical and Actuarial Sciences ACTUARIAL SCIENCE 2053

Mathematics for Financial Analysis -- 2018-19

| Instructor                        | Sec | Day/Time                            | Location | email                    | Office/Phone           |
|-----------------------------------|-----|-------------------------------------|----------|--------------------------|------------------------|
| Mr.Steve Kopp                     | 001 | MWF - 11:30- 12:20                  | NCB 113  | kopp@stats.uwo.ca        | WSC 284/x86288         |
| Mr. Joe<br>Raaymakers             | 002 | Tu - 9:30-11:20<br>Th - 10:30-11:20 | WSC 55   | jraaymakers@stats.uwo.ca | WSC 107                |
| Mr. Xing Jiang<br>(Kings College) | 570 | Tu - 11:30-1:00<br>Th - 11:30-1:00  | LH 101   | xjiang32@uwo.ca          | LH 205<br>519-433-3491 |
| Mr. Xing Jiang (Kings College)    | 571 | Tu - 3:00-4:30<br>Th - 3:00-4:30    | LH 103   |                          | x4530                  |

#### **Prerequisites:**

Grade 12U calculus (or equivalent), PLUS one full university level course (or 2 half courses) from Mathematics, Applied Mathematics, Calculus, or Linear Algebra

#### **Anti-requisites:**

Actuarial Science 2553A

Students are advised that they are responsible to ensure that they possess the necessary prerequisites (or have written special permission) and that de-registration may occur at <u>any time</u> if they lack the prerequisite or have taken an anti-requisite course.

#### Textbooks (both are available in the UWO bookstore)

- "Mathematics of Finance", NEW 8th Edition, by Brown-Kopp (about \$95)
- Study note package (about \$25)

**Course Outline** (course is divided into 2 terms):

| Text                  | Chapter | Topic   |  |
|-----------------------|---------|---|--|
| 1. Textbook           | 1       | Simple Interest                                     |  |
|                       | 2       | Compound Interest (skip section 2.10)               |  |
|                       | 3       | Simple Annuities                                    |  |
|                       | 4       | General Annuities                                   |  |
|                       | 5       | Repaying A Debt                                     |  |
|                       | 6       | Bonds (skip Serial Bonds of section 6.7)            |  |
| 2. Textbook           | 7       | Business Decisions, Capital Budgeting, Depreciation |  |
| 3. Study Note Package | 8       | Fixed Income Investments                            |  |
|                       | 9       | Probability and Life Tables                         |  |
|                       | 10      | Life Annuities                                      |  |
|                       | 11      | Life Insurance                                      |  |
|                       | 12      | Life Insurance Expenses                             |  |

#### **Term Tests**

- 1. Test 1: Friday, October 26, 2018 -- 6 to 8 pm topics to be posted on OWL
- 2. Test 2: Friday, March 1, 2019 -- 6 to 8 pm topics to be posted on OWL

The format will most likely be multiple-choice questions. A formula page will be provided for both tests.

NOTE: There is NO makeup test to either Test 1 or Test 2. If you miss either test (with a valid reason), the 18% weight will be moved to the mid term exam (if you miss Test 1) or the final exam (if you miss Test 2). You should think twice (or 3 times) before deciding to miss a test.

#### **Mid Term Exam**

To be scheduled during the Christmas Exam period

Chapters 1, 2, 3, 4, 5, and part of chapter 6

• The midterm exam will cover all material from the first term, including material that was tested on Test 1. It will be a 3-hour exam that may either be multiple choice questions OR a combination of multiple choice and short written answer questions. A formula page will be provided.

#### **Final Exam**

## Scheduled for the final exam period.

Rest of Chapter 6, all of chapters 7, 8, 9, 10, 11, 12

• The final exam will be a 3-hour exam that may either be multiple choice questions OR a combination of multiple choice and short written answer questions. A formula page will be provided. It will be based on material covered in class only since the midterm exam but will include material from the 2<sup>nd</sup> term test.

### You will also need a pocket calculator for the tests and the exams.

#### **In-class Quizzes**

There will be 8 (4 per term) short written answer question quizzes that will be given at the very start of class on the following **Wednesdays** (section 001) **OR Tuesdays** (section 002):

| 1 | September 26, 2018 (001) | 5 | January 23, 2019 (001) |
|---|--------------------------|---|------------------------|
|   | September 25, 2018 (002) |   | January 22, 2019 (002) |
| 2 | October 17, 2018 (001)   | 6 | February 6, 2019 (001) |
|   | October 16, 2018 (002)   |   | February 5, 2019 (002) |
| 3 | November 7, 2018 (001)   | 7 | March 13, 2019 (001)   |
|   | November 6, 2018 (002)   |   | March 12, 2019 (002)   |
| 4 | November 28, 2018 (001)  | 8 | April 3, 2019 (001)    |
|   | November 27, 2018 (002)  |   | April 2, 2019 (002)    |

- The quizzes will start <u>right</u> at the start of the class on the above dates and you will have 15 minutes to complete the assigned question(s) **do NOT** be late for class on these dates as you will NOT be given extra time
- The quizzes will consist of 2 questions (or perhaps 1 question with multiple parts) that will be based on material covered over the past 2-3 weeks of classes
- You will show ALL your work in solving the question (as part marks will be available)
- The quizzes will be out of 8 marks you will get 2 out of 8 just for signing your name and handing in a blank answer
- Only your <u>best 6 out of 8 quizzes will count</u> in your final mark (so you can miss up to 2 quizzes for any reason and you do not need any medical documentation).

#### **Evaluation**

|                           | Original | If you do poo | orly on one test |
|---------------------------|----------|---------------|------------------|
| Quizzes (best 6 out of 8) | 10%      | 10%           | 10%              |
| Test 1                    | 18%      | 9%            | 18%              |
| Mid Term                  | 27%      | 36%           | 27%              |
| Test 2                    | 18%      | 18%           | 9%               |
| Final Exam                | 27%      | 27%           | 36%              |

The marking scheme that gives a student the higher final mark will be the one used for that student.

# **Course OWL Web Page**

The web page will contain:

- 1. A copy of this course outline
- 2. Copies of tests and exams from the previous year (with solutions)
- 3. Solutions to the exercises in the 8<sup>th</sup> edition of the textbook (as pdf files)
- 4. Weekly updates and information about the course that you need to know
- 5. Daily class notes (which will be incomplete to be filled in during the classes) and other things that are relevant to the course.
- 6. Marks of quizzes and tests as they are marked.

## **Course Objectives**

This course is <u>not</u> intended to make you financial geniuses or to suggest what investments or insurance products you should be buying.

Instead, the objective of this course is to show you how you can do many useful financial calculations yourself, either using a calculator, pen and paper OR using a computer spreadsheet. <u>Some</u> of the calculations you will be able to do by the end of the course include:

- 1. Accumulating & discounting a single sum of money using either simple or compound interest
- 2. Accumulating & discounting a series of payments made at equal time intervals using compound interest
- 3. Calculating loan payments, including mortgage payments
- 4. Depreciating physical assets
- 5. Determining the rate of return on an investment
- 6. Determining the price of a bond or the rate of return on a bond
- 7. Understanding the yield curve and the risks involved with a fixed income investment

In the last part of the course you will be introduced to the fundamentals of financial calculations involving life contingencies. You will be able to:

- 1. Perform calculations involving probabilities of living or dying within a certain period of time
- 2. Calculate how much money you need at a certain age to purchase an annuity paying you a certain amount of money every year or every month for the rest of your life
- 3. Calculate the premium to be paid for a certain type of life insurance policy

Your ability to do all the above (and more) will be evaluated through written answer questions on the in-class quizzes and through a combination multiple choice/written answer questions on two tests and two exams.

# **APPROXIMATE** Weekly Course Outline:

| Week - 2018           | Section  |  |
|-----------------------|--|--|
| Sept 6-14             | Accumulating/discounting simple interest (sect 1.1-1.2)                      |  |
| Sept 17-21            | Equations of value, partial payments, simple discount (section 1.3 to 1.5)   |  |
| Sept 24-28            | Accumulating/discounting with compound interest, equivalent rates,           |  |
|                       | fractional periods (section 2.1-2.4)   |  |
| In                    | -class Quiz #1 – Tues/Wed, September 25/26 at start of class                 |  |
| Oct 1-5               | Determining the time and interest rate, equations of value, changing         |  |
|                       | rates, other applications (section 2.5 to 2.10)                              |  |
| Oct 8-12              | FALL break   |  |
| Oct 15-19             | Ordinary annuities – accumulated value (section 3.1, 3.2)                    |  |
| I                     | In-class Quiz #2 – Tues/Wed, October 16/17 at start of class                 |  |
| Oct 22-26             | Ordinary annuities – present value (section 3.3)/ REVIEW                     |  |
| Test 1 – Friday, Octo | ober 26 – 6:00 to 8:00 pm (2 hours) – Chapters/Sections TBA                  |  |
| Oct 29-31, Nov 1-2    | Other Annuities (section 3.4); Determining term/rate (section 3.5, 3.6)      |  |
| Nov 5-9               | General annuities, mortgages, Perpetuities, (section 4.1-4.2-4.3)            |  |
|                       | In-class Quiz #3 –Tues/Wed, November 6/7 at start of class                   |  |
| Nov 12-16             | Varying annuities (section 4.3), Amortization (section 5.1)                  |  |
| Nov 19-23             | Outstanding balance, Refinancing, Sum of digits (section 5.2, 5.3, 5.4)      |  |
| Nov 26-30             | Sinking Funds (sect 5.5/5.6/5.7) Bonds – Purchase price and callable         |  |
| 1.01 20 00            | bonds (sections 6.1/6.2/6.4)   |  |
| In                    | n-class Quiz #4 – Tues/Wed, November 27/28 at start of class                 |  |
| Dec 3-7               | Premium and Discount, (section 6.3); REVIEW                                  |  |
|                       | be scheduled during the December Exam period (3 hours)                       |  |
| Week - 2019           | be selected during the December Laum period (5 hours)                        |  |
| Jan 7-11              | Price between dates, rate of return, other bonds (section 6.5, 6.6, 6.7)     |  |
| Jan 14-18             | Net present value, internal rate of return, capitalized cost (sects 7.1-7.3) |  |
| Jan 21-25             | Depreciation (section 7.4); Fixed income investments, yield curve,           |  |
|                       | forward interest rates (sections 8.1, 8.2),                                  |  |
| I                     | n-class Quiz #5 – Tues/Wed, January 22/23 at start of class                  |  |
| Jan 28-Feb 1          | Types of risks (section 8.3); Duration, convexity (sections 8.4 to 8.7)      |  |
| Feb 4-8               | Probability, life tables probabilities (section 9.1 to 9.5)                  |  |
|                       | In-class Quiz #6 – Tues/Wed, February 5/6 at start of class                  |  |
| Feb 11-15             | Expectation of life, select mortality (section 9.6 and 9.7)                  |  |
|                       | Feb 18-22 – Reading Week   |  |
| Feb 25-Mar 1          | Pure endowments (section 10.1/10.2/10.3); Review                             |  |
|                       | rch 1 – 6 pm to 8 pm (2 hours) – Chapters/Sections TBA                       |  |
| Mar 4-8               | Whole life, temporary and deferred, (section 10.4-10.6)                      |  |
| Mar 11-15             | Varying annuities, life annuities payable more than once a year, whole       |  |
|                       | life insurance (section 10.7, 10.8, 11.1)                                    |  |
|                       | In-class Quiz #7 – Tues/Wed, March 12/13 at start of class                   |  |
| Mar 18-22             | Whole life insurance (section 11.2, 11.3)                                    |  |
| Mar 25-29             | Net annual premiums, term and endowment insurance (sect 11.3 to 11.6)        |  |
| Apr 1-3               | Deferred/varying insurance (section 11.6 to 11.8)                            |  |
|                       | In-class Quiz #8 – Tues/Wed, April 2/3 at start of class                     |  |
| Apr 4-9               | Expenses; Types of life insurance expenses (section 12.1, 12.2)/ Review      |  |
|                       | scheduled in final exam period   |  |
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#### **Classroom Environment**

courtesy, respect and honesty.

We have adopted a "Mutual Expectations" policy governing the classroom environment and all work submitted by students. [The full text of the policy can be found on the Statistical and Actuarial Science departmental web page, <a href="http://www.uwo.ca/stats">http://www.uwo.ca/stats</a> or go directly to the web page: <a href="https://www.uwo.ca/stats/undergraduate/mutual-expectations.html">https://www.uwo.ca/stats/undergraduate/mutual-expectations.html</a>]. In summary, all interactions between students and faculty should be governed by the principles of

**Students are encouraged to ask questions in the class.** But cell phones use should be limited to CLICKER questions only., Also any unnecessarily loud talking among students is to be discouraged. The goal is to reduce any behaviour by students that may disrupt other students

# What Do You Do if You Miss a Course Requirement Due to Illness or Special Circumstances?

If you are unable to meet a course requirement due to illness or other serious circumstances, you must provide valid medical or supporting documentation to the Academic Counselling Office of your home faculty as soon as possible and contact your instructor immediately. If you are a Social Science student, the Academic Counselling Office of the Faculty of Social Science is located in SSC Room 2105, or can be contacted at ssaco@uwo.ca.

<u>For in-class quizzes</u>: There are NO make ups to any of the quizzes, so if you miss one (or two) it will be one of the two quizzes that will not count towards your final mark. If you miss a third quiz, it will count as a mark of ZERO. You do not need to get in contact with your Faculty or your instructor if you miss a quiz (or two).

<u>For Tests</u>: If you miss a test for a valid reason, you must go to your Faculty with proof as to why you missed the exam. There are no makeup tests. The weight of the missed test will be moved to either the midterm exam (if Test 1 was missed) or the final exam (if test 2 was missed).

<u>For Midterm/Final Exam</u>: If you miss an exam for a valid reason, you must go to your Faculty with proof as to why you missed the exam. A makeup exam date will be arranged for all students who missed the exam with a valid reason.

For further information, please consult the university's medical illness policy at <a href="https://www.uwo.ca/univsec/pdf/academic\_policies/appeals/accommodation\_illness.pdf">https://www.uwo.ca/univsec/pdf/academic\_policies/appeals/accommodation\_illness.pdf</a>

If you require academic accommodation due to illness, you should use the Student Medical Certificate when visiting an off-campus medical facility. The form can be found here: <a href="http://www.uwo.ca/univsec/pdf/academic\_policies/appeals/medicalform.pdf">http://www.uwo.ca/univsec/pdf/academic\_policies/appeals/medicalform.pdf</a>

Or, request a Record's Release Form (located in the Dean's Office) for visits to Student Health Services.

The website for Registrarial Services is <a href="http://www.registrar.uwo.ca">http://www.registrar.uwo.ca</a>.

#### Attendance

The department of Statistical and Actuarial Sciences views classroom attendance as a very important part of the learning process. You are expected to attend all classes. You are advised that excessive absenteeism may result in being debarred from the final examination.

#### Policy on e-mail communication

E-mail can be an efficient and effective way to communicate with your Professor, but it should be <u>used very rarely</u>, only to provide us with information or to ask a question that requires a very brief response. We do not wish to see emails that ask "What did I miss in class today?". For more lengthy discussions, you should raise questions after class or during office hours, or make a separate appointment if necessary. Please remember that we will only read e-mails from your UWO student account. E-mails from other accounts (e.g. hotmail, yahoo, etc.) will not be read. **Please conduct yourselves professionally if you choose to e-mail your Professor.** 

#### **Support Services**

Please contact the course instructor if you require lecture or printed material in an alternate format or if any other arrangements can make this course more accessible to you. You may also wish to contact Services for Students with Disabilities (SSD) at 661-2111 ext. 82147 if you have questions regarding accommodation.

The policy on Accommodation for Students with Disabilities can be found here: www.uwo.ca/univsec/pdf/academic\_policies/appeals/accommodation\_disabilities.pdf

The policy on Accommodation for Religious Holidays can be found here: <a href="http://www.uwo.ca/univsec/pdf/academic\_policies/appeals/accommodation\_religious.pdf">http://www.uwo.ca/univsec/pdf/academic\_policies/appeals/accommodation\_religious.pdf</a>

Learning-skills counsellors at the Student Development Centre\_are ready to help you improve your learning skills. They offer presentations on strategies for improving time management, multiple-choice exam preparation/writing, textbook reading, and more. Individual support is offered throughout the Fall/Winter terms in the drop-in Learning Help Centre, and year-round through individual counselling: http://www.sdc.uwo.ca

Students who are in emotional/mental distress should refer to Mental Health@Western for a complete list of options about how to obtain help: http://www.health.uwo.ca/mental\_health

Additional student-run support services are offered by the USC: <a href="http://westernusc.ca/services">http://westernusc.ca/services</a>.

# Accessibility

Please contact the course instructor if you require lecture or printed material in an alternate format or if any other arrangements can make this course more accessible to you. You may also wish to contact Services for Students with Disabilities (SSD) at 661-2111 ext. 82147 if you have questions regarding accommodation.